Determinants and Predictions of Risks of Diseases in Ages: Logistic Regression Models versus Deep Neural Network Models\*

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#### **Abstract**

Prediction of risks of various diseases and identification of factors that influence these risks are important for public policies and disease diagnosis in healthcare. The biomedical literature suggests that much of an individual's later life health outcomes is programmed at early stages of life. The programming is strongly modulated by epigenetic inputs throughout life such as psychological, financial, social or chemical stress, diets, smoking, substance use, and exercising, with stronger effects imparted in early stages of life. Traditionally predicting effects of these factors on risks of diseases is statistically examined using the logistic regression framework. Deep neural network models have shown superior predictive performances in other fields and can be used in the present context. This paper compares the effectiveness of these two approaches in quantitatively predicting these risks as a function of the observable variables and in identifying the influential variables that strongly affect the risks with the Health and Retirement Studies (HRS) data. I compare its predictive performance with performances of statistical procedures using confusion matrix and other indicators and then compare their predictions of policy outcomes.

<sup>\*</sup>Draft prepared for presentation at the 85th birthday celebration of Professor Kirith Parikh. Professor Parikh and I crossed roads on many occasions. He has worked on many fields with bearings on public policies for India. I have not directly worked with him, but I have known Professor Parikh's work through his collaboration with my Professor and mentor, the late Professor T.N. Srinivasan and his mentoring of my classmates and contemporaries at the Indian Statistical Institute, New Delhi. I have felt his academic contributions, including his contributions in the architectural designs of the Indian Statistical Institute, New Delhi and Indira Gandhi Institute of Development Research, Mumbai where I have spent some time. This paper is dedicated in loving memory of my mentor and professor the late T.N. Srinivasan. **Disclaimer:** The views, thoughts, and opinions expressed in the paper belong solely to the author, and do not necessarily represent the views of any institution, other group or individual..

# **1.** Introduction

The prediction of risks of various chronic diseases and identification of important factors for such risks are important issues in healthcare industry and public policies. For instance, in healthcare industry, the caregivers such as doctors and nurses may look at symptoms and medical history of an incoming patient to determine what diseases are most likely for the patient and then follow-up further tests and treatments. For public policy, prediction of risks of various diseases in communities can help build up infrastructure to deal with the health problems of the community. Various diseases affect the probability of disability, work loss and early death. Estimating those risks can help better policies for social insurance programs such as disability insurance programs and for private insurance programs to calculate the insurance premiums or for the regulators to regulate the private health insurance companies. What factors are important for development of diseases over a lifespan? Should we be using statistical models or machine learning predictive models for predictions? Public policies influence many of the individual characteristics that determine disease risks. From public policy perspective, it is also important to estimate the quantitative effect of such characteristics on the likelihood of various diseases, which can help designing policies to reduce health inequality among social groups or improve health of the general population. I use the Health and Retirement Surveys data for empirical exploration of the above issues in this paper.

The biomedical literature suggests that much of an individual's later life health outcomes is programmed at early stages of life. The programming is strongly modulated by the epigenetic inputs created by the environment in mother's womb at prenatal stage and by the environment at early postnatal ages. The most important epigenetic factor is stress of any kind – psychological, financial, social and chemical. Other significant factors are medical care, diets, smoking, substance use, and exercising. These modulating factors are important throughout life, with stronger effects imparted in early stages of life. At the cellular level, aging and the incidence of age related diseases occur due to cellular senescence — i.e., after a certain number of cell divisions, it stops dividing or have defective replications, causing tissues or organs to increasingly deteriorate over time. What are the critical periods or the developmental milestones in life-cycle that program the motions of health developments over the lifespan of an individual?

<span id="page-2-0"></span>Research along this line began with the striking findings of Barker [\(Barker, 1990](#page-24-0); [Barker,](#page-24-1) [1998\)](#page-24-1) and later of [Gluckman et al. \(2008](#page-25-0)). They found strong association between birth weight and many later life chronic diseases, including hypertension, coronary artery diseases, type 2 diabetes, and osteoporosis. Many other studies find that much of health developments in later life is determined very early in life — specifically during the prenatal period, right after conception, i.e. in the womb. Sometimes it is said in social sciences that inequality begins in the womb. The effect of an environmental stress in the womb on later life diseases and developmental outcomes is known as *programming*. [Gluckman et al. \(2008](#page-25-0)) observes that "like the long latency period between an environmental trigger and the onset of certain cancers, the etiology of many later life diseases such as cardiovascular disease, metabolic disease, or osteoporosis originate as early as in the intrauterine development and the influence of environments that created by the mother." Many studies in social sciences find that low socioeconomic status (SES) are associated with inflammation, metabolic dysregulation, and various chronic and age-related diseases such as type 2 diabetes, coronary heart disease, stroke, and dementia, and that low SES create epigenetic changes in individuals that lead to faster biological aging even after controlling for health-related behaviors such as diet, exercise, smoking, alcohol consumption, or access to quality health care, see for evidence, [Simons et al. \(2016\)](#page-26-0).

Generally prediction and estimation of risks of disease are carried out in statistical multinomial framework. In recent years machine learning techniques, especially the deep neural network predictive models are producing much superior predictions compared to the statistical models. For instance, [Chen et al. \(2017\)](#page-24-2) used patient data from various hospitals in china to fit a neural network model and achieved high prediction accuracy rates. Machine learning techniques are used for prediction and selection of factors in cancer research, see [Kourou](#page-26-1) [et al. \(2015\)](#page-26-1) for a survey of these models. It is known that a feed-forward deep neural network model with a sufficient number of neurons in the hidden layers can approximate any function as closely as desired. That is, an MLP is one of the best *universal function approximator*, see [\(Hornik et al., 1989;](#page-25-1) [Cybenko, 1989\)](#page-24-3). To many social scientists, the machine learning techniques are mysterious. The purpose of this paper is to explain the structure of deep feed-forward neural network models, how they differ from statistical models in terms of prediction of risks and identification of important factors of the risks.

The rest of the paper is organized as follows. In section [2](#page-3-0), I describe two modeling paradigms, the multinomial logistic regression model from the statistics literature and the

<span id="page-3-1"></span>deep neural network model from the machine learning literature. In section [3,](#page-11-0) I describe the Health and Retirement Study data set and the common set of variables that I use for fitting models in both frameworks. In section [4,](#page-15-0) I report the numerical findings on predictive performance and variable importance. In section [5,](#page-20-0) I discuss the issues in the dynamic context. Section [6](#page-22-0) concludes the paper.

# <span id="page-3-0"></span>**2.** Two modeling paradigms

Empirical investigation of our main issues — prediction of risks of various diseases and identification of factors that influence these risks – involves two types of statistical models: *explanatory models* and *predictive models*. To explain it briefly using a unified general framework covering problems in other fields, I use the terminology and notation in [Shmueli](#page-26-2) [\(2010](#page-26-2)). Most problems postulate a relationship,  $\mathscr{Y} = \mathscr{F}(\mathscr{X})$ , where  $\mathscr{X}$  is a vector of certain input constructs related to a certain set of output constructs *Y* through some theoretical hypothesis or theories represented by  $\mathscr F$ . In most situations including the present, the underlying theory such as biology of aging and disease developments of humans provide qualitative relationships, not quantitative specifications in terms of measurable variables and a mathematical function. A statistical or econometric model operationalizes this relationship in terms of a vector of observable input random variables  $X$  and a vector of output random variables Y with a mathematical function  $Y = f(X)$ . Depending on data availability or collection problems, one may have many choices for the set of input variables  $X$ , and outcome variables  $Y$  and the functional form  $f$  relating them, each configuration gives one model (see for instance various types structural equation model specifications in [Hair et al.](#page-25-2) [\(2017](#page-25-2)), and [Pearl \(2009](#page-26-3))).

In the present context,  $\mathscr X$  consists of individual genetic make-up and epigenetic factors over the life-span such as stressors that govern the cell divisions producing various health outcomes over time. These are not directly observable or we do not have information on individual genomes. I use various observable input variables  $X$ , some of which can be improved with public policies and some with individual behaviors. Our outcome health variable is a single discrete random variable  $Y$  denoting an individual's health status in middle age. The set of health statuses is  $\{1,2,3,4,5\}$ , where  $1 =$  normal health,  $2 =$  Cardiovascular disease,  $3 =$  Cancer,  $4 =$  Other single disease,  $5 =$  comorbidity. These are discrete values without

distinguishing the degree of severity. In an explanatory model,  $f$  is a causal function, i.e., it assumes  $X$  causes  $Y$ . In a predictive model  $f$  denotes the association between  $X$  and  $Y$ .

Both statistical models and neural network models approximate the unknown function  $Y = f(X)$  with a parametric function  $Y = f(X; \beta)$  from some parametric family of functions and chooses the best one that minimizes the expected value of a loss function,  $\mathscr{L}(Y, f(X))$ . Statistical models generally specify parametric functions in such a way that parameters can directly provide the quantitative effect of an input variable on the outcome variables. In the next subsection, I describe the most widely used such model, multinomial logistic regression model.This the statistical model I use in this paper.

#### **2.1.** The Multinomial logistic regression model

The multinomial logistic regression model assumes that the conditional probability distribution of Y given X belongs to a family of exponential distributions with parameters  $\beta$ , giving the following specification,

<span id="page-4-1"></span>
$$
log\frac{P(Y=k|X)}{P(Y=1|X)} = X'\beta_k, \ k = 2, ..., 5.
$$
 (1)

Taking  $\beta_1 = 0$ , i.e., taking the normal health as the baseline or reference outcome, the above is equivalent to,

<span id="page-4-0"></span>
$$
Y = \arg \max_{k=1,\dots,5} \frac{\exp\left(X'\beta_k\right)}{\sum_{j=1}^5 \exp\left(X'\beta_j\right)} \equiv f(X;\beta) \tag{2}
$$

In the above specification, the parameter  $\beta_{jk}$ , the  $j^{th}$  component of  $\beta_k$  corresponding to the input variable  $X_j$  has the interpretation that a unit increase in  $X_j$  will change the logodd of disease k by  $\beta_{ik}$ . That is,  $exp(\beta_{ik})$  is the *odds-ratio* of outcome k and outcome 1 associated with a one-unit increase in the input  $X_j$ . In other words, a unit increase in  $X_j$  will change the likelihood of disease k by  $exp(\beta_{ik})$  times the likelihood of normal health. This specification has the advantage that statistical estimate of the  $\beta_{jk}$  using a dataset provides both statistical and numerical significance of this variable, and thus helps one to decide which input variables are most significant for outcomes.

## **2.2.** The deep neural network model

Neural network is a highly parameterized universal function approximator of the form  $y =$  $f(x; w)$ , where x is a set of inputs, and w is a vector of parameters. This is of the same nature as a statistical model. More precisely, suppose we have data on a set of individuals of the type  $\{(x_i, y_i), i = 1, ..., n\}$ , where  $x_i$  is a vector of individual  $i$ 's characteristics, and  $y_i$  is a vector of the individual's output levels and  $w$  is a set of parameters common to all individuals. The output could be a categorical variable for classification problems, it could be a probability distribution over finite classes, as in our case, or it could be a continuous variable for regression problems. The data generating process for  $y$  as a function of x, is not known. The goal is to approximate the unknown data generating function using the observed data. This is the problem that both statistics and neural network deal with. In neural network, the problem is to design a *neural network architecture* of the approximating function  $y = f(x, w)$  and find a suitable *learning algorithm* to learn the parameters w of the network using a training set of examples to minimize a loss function. This trained network can then be used to predict  $y$  for given characteristics  $x$  of any individual.

The popularity and wide applicability of neural network lies in the fact that it designs the approximator in a hierarchy of functions, joined together by compositions of functions, that renders good properties in terms of ease of computation and closeness of the approximated function to the true data generating function. Most neural network models have the following type of hierarchical functional form:

$$
y = f(x; w) \equiv f_{w}^{L} \circ \dots \circ f_{w_{1}}^{1}(x).
$$
 (3)

Each function corresponds to a layer of artificial neurons. The role of each neuron is to perform simple calculations and then pass the result on to the next layer of neurons.

Neurons in each layer get signals which are the outputs of the neurons of the previous layer (also known as activation levels) that it is connected with. It sums them, I denote this sum by z and apply an activation function to produce an output also known as *activation level*, which I denote by  $a$ . The activation level  $a$  will then be passed on as an input to a neuron that it is connected to in the next layer. The neurons of the last layer will compute the output level taking the activation levels of the connected neurons of the previous layer.

For graphical illustration, consider a simple neural network architecture depicted in [Fig-](#page-7-0)

[ure 1](#page-7-0). It has three layers — layer 0: input layer, layer 1: hidden layer, and layer 2: output layer. Last layer in the text is denoted by L, and hence  $L = 2$ . Layer 0 has three input neurons. The second layer has 4 neurons. and last layer has two neurons corresponding to the two output levels, in our case probability of two events. In this neural network, the hierarchical function specification is of the form:

$$
f(x; w) = \sigma^2 \left( z^2 \left( \sigma^1 \left( z^1(x, w^1) \right), w^2 \right) \right) \equiv f_{w^2}^2 \circ f_{w^1}^1(x). \tag{4}
$$

The function  $z^i(a^i, w^i) = w^i \cdot a^{i-1}$  at each layer i is a linear aggregator. In the notation,  $z^i$  is a vector of functions, each component of which corresponds to a neuron of the *i*-th layer. The function  $\sigma^i$  is a squashing function of the same dimension as  $z^i$ , each component having the same function real valued function of one variable, known as *activation function*. An activation function squashes the value of  $z^i$  to a range such as to the range  $(0, 1)$  by the *sigmoid* activation function  $(f(x) = 1/(1 + e^{-x}))$ , to the range  $(-1, 1)$  by the *tanh* activation function (tanh(x) = 2sigmoid(2x) – 1) and to the range  $[0, \infty)$  by the most widely used *ReLu* function  $(f(x) = max(0, x))$ . In many situations, better and faster results emerge from the ReLu function because it does not activate all the nodes in the following layers during training. I have mentioned about only a few widely used ones. There are many other ones. In fact, any function can be an activation function.

For the output layer, which is the last layer of the network, when the goal is to estimate the probability or the value of a binary outcome variable, one uses the sigmoid function; when the goal is to estimate the probability or the outcome of a categorical output variable, one uses the *softmax* function. Denoting a k dimensional vector as  $\tilde{z} = (z_1, ..., z_k)$ , the softmax function is a k variate function  $\sigma(\tilde{z}) = (\sigma_1(\tilde{z}), ..., \sigma_k(\tilde{z}))$  defined as

$$
\sigma_j(\tilde{z}) = \frac{e^{z_j}}{\sum_1^k e^{z_i}}, j = 1, ..., k.
$$
\n(5)

This is the function used in the multinomial logit model, see [Eq. \(2\)](#page-4-0). Here  $z_j$ 's are nonlinear functions of input variables, e.g. the composite vector function  $z_j \equiv z_j^2(X; w)$  in our example above and in the [Figure 1](#page-7-0) below; whereas in the multinomial logit model Eq.  $(2)$ , it is a linear function  $z_j \equiv X'\beta_j, j = 1, ..., k$ .

<span id="page-7-1"></span>The value of an activation function,  $a^i = \sigma^i(z^i)$  is known as the *activation level* of the neurons of the *i*-th layer. The activation levels of the 0-th layer,  $a^0 = x$ , the inputs, fed to the neural network from outside. The operation on the right is also performed componentwise for each neuron at the  $i$ -th layer it computes the weighted sum of the activation levels (outputs) of the neurons of the previous layer that the neuron of the  $i$ -th layer is connected to. The weights used are specific to the neuron of the  $i$ -th layer. An activation function  $\sigma^i$  which generally taken to be same for all the neurons of the *i*-th layer) is applied to this aggregated value  $z^i$ . These activation functions do not have any unknown parameters that need to be estimated. These two computations—aggregation and activation—are shown as a composite mapping  $f_{w^i}^i$  for the neurons of the *i*-th layer.

<span id="page-7-0"></span>

Figure 1: A feed-forward deep neural network architecture.

There are different types of neural networks, depending on the functional form of  $f$  in [Eq. \(6\)](#page-8-0). A *deep feed forward neural network*, also known as a *feed forward neural network with hidden layers* or as a *multi-layer perceptron (MLP)* is a network architecture in which there is no feedback of any neurons to itself or to others in the same layer. See [Goodfellow et](#page-25-3) [al. \(2016](#page-25-3)) for detailed descriptions of these terminologies and workings of the feed-forward deep neural network models of various types and [Graves \(2012](#page-25-4)) for recurrent neural models of various types, which I will not describe or use in this paper. The activation levels of the neurons only feed forward to the neurons in the next layer. This is the reason also why these types of neural networks are called feed forward neural network, as opposed to

<span id="page-8-1"></span>the *recurrent neural network* which allows feedback of a neuron to itself. The MLP has good computational properties and an MLP is a great universal functional approximator: It is shown [Hornik et al. \(1989\)](#page-25-1) that with a sufficient number of layers in a hidden layer can approximate a function to any level of precision desired. So a MLP can be used to approximate the true data generating process as closely as one wants. How does one find such a network, i.e., how does one choose the weights of the network.

I take the categorical cross entropy as the loss function. I have tried the Kullback-Leibler divergence as the loss function and findings are similar and not reported.

To get a good approximation, the artificial neural network contains hundreds of thousands of deep parameters  $w$ , how does one train the network, i.e., how to learn the best set of parameter values using the data at hand. The learning is done by choosing the weights to minimize a loss function together with a non-negative regularization term (in statistical term a regulerization term corresponds to a shrinkage estimator) to avoid over-fitting.

<span id="page-8-0"></span>
$$
\frac{1}{n}\sum_1^n(\mathscr{L}(y_i,f(x_i;w)))+\lambda C(w). \hspace{1.5cm} (6)
$$

In the present context of learning about a probability distribution over the discrete set of health outcomes, it is appropriate to take the loss function to be negative log-likelihood of the sample and the additive regularization term  $C(w)$  to be  $||w||_1$  known as  $L_1$  regularizer, or to be  $||w||_2$ , known as the  $L_2$  regularizer or take a convex combination of the two known as the *elastic-net* or  $L_1 L_2$  regularizer. The choice of  $w$  to minimize the loss is done by a gradient descent method. The neural network architecture [Eq. \(6\)](#page-8-0) yields a very convenient fast and automatic computation of the gradients  $\partial \mathcal{L}/\partial w$  using an algorithm known as the back-propagation algorithm, used pretty much in all types of neural networks. The steps in this algorithm are as follows:

#### **Backpropgation Algorithm**

- Step 0: Assume an initial value for the weights  $w$ .
- Step 1: Compute all the activation levels starting at the input layer, i.e.,  $f_w^1(x)$ forward through the layers  $2, 3, ..., L$  in [Eq. \(6\)](#page-8-0), i.e., go through layer superscripts forward.
- Step 2: Compute gradients of the weight parameters  $w$  of various layers, starting from the last layer, backward in layers, i.e., decreasing order in the subscripts in Eq.  $(6)$ .
- Step 3: Adjust weights using a steepest descent rule.
- Step 4: If the difference between the initial weights and these adjusted weights is within a tolerance limit, stop, and take these adjusted weights as the optimal weight estimate; otherwise, reset the initial weights to these adjusted weight, and go to Step 1.

### **2.3.** Estimation and prediction methods in two paradigms

In a parametric model such as in Eq.  $(1)$ , a parameter will provide the effect of the input variable on an outcome variable, only if the model is *statistically identified* in the sense that given  $P(Y|X, \beta)$ , there exists a unique  $\beta$ . By parameterizing the odds-ratio in [Eq. \(1\)](#page-4-1), the multinomial logit model is statistically identified.

Whether a parametric model is statistically identified or not, it can produce predictions of outcomes, by predicting the outcome to be that which has the highest probability, i.e., arg max ${}_{k}P(Y=k|X,\beta)$ . Other rules are possible too.

In statistics, to estimate parameters of a model from a sample of observations, one takes negative the log-likelihood function as the loss function  $\mathscr{L}(Y, f(X; \beta))$  and minimizes the expected value of the loss function taken with respect to the empirical distribution, i.e., one maximizes  $\sum_{1}^{n}$  $T_1^n(\mathscr{L}(y_i, f(x_i; \beta))),$  where  $y_i, x_i, i = 1, ..., n$  is a random sample. This optimum estimator  $\hat{\beta}$  is the *maximum likelihood estimator*. Under the assumption that the true data generating process, i.e., the true f is a member of the parametric family, the maximum likelihood estimator  $\hat{\beta}$  is asymptotically efficient, consistent and asymptotically unbiased. In some cases, these properties hold in the small sample as well. These properties are uti<span id="page-10-0"></span>lized to carry various hypothesis testing about the parameters such as if a parameter or a set of parameters is statistically significant. For instance, we can look at the p-values to determine if a variable has statistically significant effect. This assumption about the true data generating process is hardly true in real life data. [Breiman \(2001b](#page-24-4)) provides a strong critique of this statistical modeling approach. He introduced algorithmic *tree based methods* such as CART and Random Forests. Other models along this line are the linear additive models [\(Hastie and Tibshirani \(2006\)](#page-25-5)), *Support Vector Machines* and neural network model. These models can be found in [Hastie, Tibshirani, and Friedman \(2009](#page-25-6)) and [Efron and Hastie](#page-24-5) [\(2016](#page-24-5)).

For the machine learning models including the deep neural network models, the estimated parameters do not have such interpretations; the models are generally not identified; and there is no straightforward procedure to identify the input variables with significant effects on the outcomes. For our deep neural network model, I adapt the *permutation importance* technique introduced by **Breiman** (2001a) for random forests models.

### **2.4.** Computational details

For both maximum likelihood estimation of the multinomial logit model in [Eq. \(1\)](#page-4-1) and the learning algorithm for the deep feed-forward neural network model in [Eq. \(6\),](#page-8-0) I split the dataset into the training dataset containing a random sample without replacement of 80 percent of the original sample and the remains as the test dataset.

For both the logistic regression model and the deep neural network model, I use the training data to fit the model and use the test data to assess the performance of these two fitted models and finally use the fitted models on the training data to compare the predicted disease risks of various social groups and talk about their policy implications. These are reported in a section following the next section that describes the dataset and the variables used in this study.

I estimate the multinomial logit model R using the package *nnet* [\(Venables and Ripley](#page-27-0) [\(2002](#page-27-0))). There are other R packages such as *glmnet* and *mlogit* that can also fit multinomial logistic models. The glmnet package, however, does not calculate the standard errors of the parameter estimates and mlogit package invloves complex data transformations.

<span id="page-11-1"></span>To fit the feed-forward neural network model, I use the Tensorflow 2.3.0 [\(TensorFlow](#page-26-4) [Developers \(2021\)](#page-26-4)) and Keras 2.4.3([Chollet et al. \(2015](#page-24-7))) in Python. While the R package nnet can also do feed-forward neural network, it is limited to only one hidden layer and it does not incorporate early stopping, regularization, random dropout to find the best possible fit of a deep neural network. The Keras and Tensorflow are more versatile. Other machine learning packages such as Pytorch, Mxnet, Scikit Learn, can be also used. I found Tensorflow and Keras to be convenient for the task of this paper.

The feed-forward deep neural network I finally chose had two hidden layers of 32 and 512 neurons. Given we have 11 input variables, and 6 output neurons for the output layer, the network consists of  $20,358$  parameters, i.e.,  $w$ 's to train. I used categorical cross entropy as the objective function, which is equivalent of the log-likelihood of the multinomial logit model. To handle over fitting, I used the reLu activation function in the two hidden layers, elastic-net or  $L_1L_2$  regularization of parameters in the two hidden layers, and early stopping, i.e., stopping early instead of training it to the maximum iterations (known as epochs) if the objection function stops improving early on. The results are reported and discussed after describing the dataset and the variables.

# <span id="page-11-0"></span>The Dataset and the construction of variables

#### **3.1.** The dataset

I use the Health and Retirement Study (HRS) dataset for empirical analysis. A lot has been written about HRS datasets — about its structure, purpose, and various modules collecting data on genetics, biomarkers, cognitive functioning, and more, see for instance([Juster](#page-25-7) [and Suzman, 1995](#page-25-7); [Sonnega et al., 2014](#page-26-5); [Fisher and Ryan, 2017](#page-25-8)). The first survey was conducted in 1992 on a representative sample of individuals living in households i.e., in non-institutionalized, community dwelling, in the United States from the population of cohort born during 1931 to 1941 and their spouses of any age. "The sample was drawn at the household financial unit level using a multistage, national area-clustered probability sample frame. An oversample of Blacks, Hispanics (primarily Mexican Americans), and Florida residents was drawn to increase the sample size of Blacks and Hispanics as well as those who reside in the state of Florida", [\(Fisher and Ryan, 2017](#page-25-8)).

<span id="page-12-0"></span>The number of respondents were 13,593. Since 1992, the survey were repeated every two years, each is referred to as a wave of survey. New cohorts were added in 1993, 1998, 2004 and 2010, ending the survey up with the sample size of 37,495 from around 23,000 households in wave 12 in 2014. The RAND created many variables from the original HRS data for ease of use. I create all the variables (with a few exceptions noted below) from the RAND HRS dataset version P. The details of the Rand HRS version P can be found in [Bugliari et al. \(2016\)](#page-24-8). I use the original cohort first interviewed in 1992 so that we have a homogeneous group of individuals with data for many years to avoid cohort effects in our analysis. This sample has the largest sample size.

The HRS data collected information on if a doctor diagnosed that the respondent had any of the severe diseases such as high blood pressure, diabetes, cancer, lung disease, heart attack, stroke, psychiatric disorder and severe arthritis.

I drop respondents who were enrolled on to disability programs before the first survey year 1992 and I also drop the spouses in the sample who were not born between 1931 to 1941, so that the respondents in our sample are between ages 51 to 61 and are not disabled or dead by the first survey year 1992. I ended up with the final sample size of 9601 for this analysis.

The table reports these statistics only up to the survey year 2006, as the individuals exited the study because of disability or death before disability or censored because they are over age 65 after this survey year. The table shows that the first period of this study in 1992 has 3026 individuals, which is 32 percent of the sample, in good health, 6483 individuals (i.e., 68 percent) in diseased health state with one-or-more chronic diseases and 92 individuals (i.e., 1 percent) left the study as they become disabled. No individuals died or were censored because of ages higher than 65 — this is the result of sample selection criterion mentioned above. In the next survey year 1994, out of 9509 non-exited individuals, 144 died without any disability. In the survey year 1998 for the first time, 727 individuals in the sample left our study because they reached ages above 65. The total number of individuals during the last survey round of 2006 before they all become older than 65 is 1581, i.e. about 16 percent of the original sample.

<span id="page-13-1"></span>

Molecular biology literature mentioned in the introduction points out that the stressors of the body cells are important determinants of the nature of cell divisions during early devel-opment and later life health outcomes.<sup>[1](#page-13-0)</sup> While those stressors cannot be directly observed or measured, many socioeconomic factors modulate those stressors and cell developments, and thus affect later life health outcomes. Furthermore, early life health developments together with health related behaviors are important determinants of later life health outcomes. Health behaviors are partly determined by cognitive and non-cognitive skills. Education level thus can affect health behaviors and health developments in later life. Education also determines earnings, which determine health related expenditures and thus health outcomes. The HRS dataset does not have prenatal or postnatal data on individuals. It has a few variables on childhood socioeconomic status, which are correlates of the stressors of the cell developments.

How does one quantify childhood SES? There is no consensus on what exactly constitutes cSES. Some studies use different sets of variables to represent cSES. For instance, [Heckman and Raut \(2016](#page-25-9)) and a few other studies use parents' education as a measure childhood SES in modeling attainment of college degree. [Luo and Waite \(2005](#page-26-6)) used Father's and Mother's education and the Family financial well-being as regressors without aggregating them into a single measure to examine how these variables affect a measure of mid-age health outcomes for the HRS sample. It is useful to have a single measure of SES. Some studies used the latent variable approach to come up with a statistically defined measure of cSES. For instance, [Vable et al. \(2017](#page-27-1)) used a number of variables from the HRS dataset to create their cSES measure. Similar to their approach, I use the latent variable statistical procedure IRT on a set of parental characteristics during the childhood of the respondents.

Other important factors are biomarkers and mental health status in the mid-ages and health related behaviors. Furthermore, the health development may vary by race and sex. I describe the construction of these variables in this subsection.

I use the Item Response Theory (IRT) from the latent variable analysis literature to construct an aggregate measure of childhood socioeconomic status, **cSES**, and two health

<span id="page-13-0"></span><sup>&</sup>lt;sup>1</sup>Genetic make-up also controls gene expressions for producing proteins that create diseases but the epigenetic factors creating the stressors are important as well.

<span id="page-14-0"></span>related behavioral traits, one capturing the propensity for using preventive care, the variable **behav\_prev**, and the other one is to measure penchant for drug and alcohol use, the variable **behave\_drink**.

The demographic variables **White** and **Female** have the standard definition. The variable **College+** is a binary variable taking value 1 if the respondent has education level of completed college and above (does not include some college), i.e., has a college degree and more and taking value 0 otherwise.

**cesd:** I used the score on the Center for Epidemiologic Studies Depression (CESD) measure in various waves that is created by RAND release of the HRS data. RAND creates the score as the sum of five negative indicators minus two positive indicators. "The negative indicators measure whether the Respondent experienced the following sentiments all or most of the time: depression, everything is an effort, sleep is restless, felt alone, felt sad, and could not get going. The positive indicators measure whether the Respondent felt happy and enjoyed life, all or most of the time." I standardize this score by subtracting 4 and dividing 8 to the RAND measure. The wave 1 had different set of questions so it was not reported in RAND HRS. I imputed it to be the first non-missing future CESD score. In the paper, I refer the variable as cesd. [Steffick \(2000\)](#page-26-7) discusses its validity as a measure of stress and depression.

**cogtot:** This variable is a measure of cognitive functioning. RAND combined the original HRS scores on cognitive function measure which includes "immediate and delayed word recall, the serial 7s test, counting backwards, naming tasks (e.g., date-naming), and vocabulary questions". Three of the original HRS cognition summary indices—two indices of scores on 20 and 40 words recall and third is score on the mental status index which is sum of scores "from counting, naming, and vocabulary tasks"—are added together to create this variable. Again due to non-compatibility with the rest of the waves, the score in the first wave was not reported in the RAND HRS. I have imputed it by taking the first future non-missing value of this variable.

**bmi:** The variable body-mass-index (BMI) is the standard measure used in the medical field and HRS collected data on this for all individuals. If it is missing in 1992, I impute it with the first future non-missing value for the variable. Following the criterion in the literature, I create the variable bmi taking value 1 if BMI> 25 and value 0 otherwise.

Now I describe the construction of the behavioral variables.

**behav** smoke: This variable is constructed to be a binary variable taking value 1 if the respondent has reported yes to ever smoked question during any of the waves as reported in the RAND HRS data and then repeated the value for all the years.

**behav** vigex: The RAND HRS has data on whether the respondent did vigorous exercise three or more days per week. I created in each time period to be 1 if the respondent did vigorous exercise three or more days per week in any of the waves and then that value is assigned to all the years.

**cSES:** This variable is a binary variable measuring childhood SES. I constructed it using the IRT procedure as follows. From the HRS data I created four binary variables using the original categorical data on family moved for financial reason, family usually got financial help during childhood, father unemployed during childhood, father's usual occupation during childhood  $(0 =$  disadvantaged and  $1 =$  advantaged), and three tertiary variables two on each parent's educational levels  $(0 = High School dropout, 1 = some college, 2 = comm)$ pleted college and higher) and third on family financial situation ( $0 = poor$ ,  $1 = average$ ,  $2 =$  well-off). I used these seven variables as items in the IRT procedure to first compute a continuous score estimate and then I define  $cSES = 1$  if the score is above mean plus one standard deviation of the scores and 0 otherwise.

**cHLTH** is a binary measure of childhood health constructed from the self-reported qualitative childhood health variable in HRS. I define **cHLTH** = 1 if the respondent reported very good or excellent, and zero otherwise.

# <span id="page-15-0"></span>**4.** Numerical findings

Childhood health status (cHLTH) is an important factor for later life health outcomes and educational attainments. cSES influences the stressors of the cells environment and thus will affect cHLTH. Apart from cSES, other factors such as nutrition and pediatric health care are important factors. We do not have data on those. I estimated a logit model of diseases with right hand side variables as childhood health, childhood socioeconomic status, college+, and other observable characteristics mentioned above.

## **4.1.** Predictions from two models

The  $(i, j)$ -th element of a *confusion matrix* gives the number of people having actually disease *i* are predicted by the model to have disease *j*, for all  $i, j = 1, \dots k$ . The numbers below in square brackets are percentages. The *accuracy* is defined as the percentage of observations in the sample are correctly predicted by the model.



<span id="page-16-0"></span>Table 1: Confusion matrix on test data using the multinomial logit model estimates on the training data

Accuracy = 38.9. Numbers in square brackets are percentages.

Confusion matrix on the test data using the parameter estimates from the training data for the multinomial logistic model is shown in [Table 1](#page-16-0) and for the deep neural network model in [Table 2](#page-17-0).

The tables show that multinomial logit model has accuracy both models have close to 40 percent accuracy, the deep neural network has slightly better overall performance, but not significantly higher. Neither models predict correctly for the disease cancer. For the disease category Other, deep neural network model perform better about 7 percent than the multinomial logit model about 2 percent.

The accuracy of about 40 percent overall performance for deep neural network with so many neurons as compared to accuracy rates of more than 95 percent accuracy rates in handwritten character recognition problems may point to the fact that the effects of the genetic factors and detailed measures of epigenetic factors throughout life are important



<span id="page-17-0"></span>Table 2: Confusion matrix on test data using deep learning model estimates on the training data

Accuracy = 39.4. Numbers in square brackets are percentages.

determinants disease risks.

## **4.2.** Influential factors in two models

#### **4.2.1.** Multinomial logit regression model

Maximum likelihood estimates and their standard errors for the multinomial logit model are reported in [Table 3.](#page-18-0) Smaller the p-value, the stronger is the statistical significance of the parameter estimate. p-values below 0.001 are marked with \*\*\*, greater than or equal to 0.001 but less than 0.01 are marked with \*\*, and greater than or equal to 0.01 but less than 0.05 are marked with \*. Starred parameter estimates of input variables for a disease are taken to be the important factors for the disease.

These estimates show that whites have lower risk of cardiovascular diseases and higher risks of other disease category.

Females have lower risk of cardiovascular diseases but higher risks of all other diseases.

Individuals who had good health in childhood have lower risks of diseases in other category and two or more diseases.

<span id="page-18-0"></span>

	$2 -$			$5-$
	Cardiovas	3-Cancer	4-other	Comorbid
Intercept	$-0.321$	$-5.005$ ***	$-0.995$ ***	0.274
	(0.214)	(0.716)	(0.228)	(0.205)
white	$-0.576$ ***	0.447	$0.296$ **	0.055
	(0.085)	(0.324)	(0.102)	(0.090)
female	$-0.172*$	$1.344$ ***	$0.549$ ***	$0.535$ ***
	(0.072)	(0.257)	(0.077)	(0.073)
childhood SES	0.003	$-0.492$	$-0.183$	$-0.046$
	(0.116)	(0.374)	(0.124)	(0.121)
childhood Health	0.107	$-0.033$	$-0.322$ ***	$-0.400$ ***
	(0.081)	(0.243)	(0.080)	(0.075)
college+	0.033	0.386	$-0.100$	$-0.155$
	(0.092)	(0.266)	(0.101)	(0.101)
bmiH	$0.668$ ***	0.120	$0.226$ **	$0.830$ ***
	(0.075)	(0.212)	(0.074)	(0.075)
CES-D	0.064	0.491	$0.809$ ***	$1.385$ ***
	(0.173)	(0.470)	(0.163)	(0.147)
cognitive scores	$-0.001$	0.026	0.008	$-0.021$ **
	(0.008)	(0.025)	(0.008)	(0.008)
smoking	0.131	$0.452*$	$0.262$ ***	$0.352$ ***
	(0.072)	(0.216)	(0.075)	(0.072)
exercising	$-0.135$	$-0.194$	$-0.074$	$-0.549$ ***
	(0.095)	(0.271)	(0.098)	(0.086)
<b>AIC</b>	18364.363	18364.363	18364.363	18364.363

Table 3: Estimates from a multinomial logistic regression model

\*\*\*  $p < 0.001$ ; \*\*  $p < 0.01$ ; \*  $p < 0.05$ .

High BMI individuals have significantly higher risk of all diseases and has no significant effect on the risk of cancer. They have the risk of cardiovascular diseases about  $exp(0.702)$ , i.e., 2.02 times higher than the risk of a low BMI individual.

Like high BMI, smoking significantly increases the risks of all diseases, except it does not have significant effect on the risk of cardiovascular diseases.

The stress measured by the variable CESD has significant effect on a single disease in other category and for comorbidity.

The risk of cancers has not many significant predictors, except that females and the

<span id="page-19-0"></span>smokers have have significantly higher risks.

#### **4.2.2.** Deep neural network model

As mentioned earlier, unlike the statistical models that produce parameter estimates and their p-values to estimate the importance and numerical effects on probabilities of outcomes, the machine learning literature does not have a sound criteria for variable selection or its effect on outcomes. I adapt the *permutation importance* technique introduced by [Breiman \(2001a](#page-24-6)) for random forests models to the present deep neural network model of multinomial output to identify influential factors as follows:

For each disease, we have computed a performance measure, the accuracy rate reported in the diagonal elements in [Table 2](#page-17-0). Denote it by  $\alpha$ . Take an input variable. If it has strong effect on the predictive power of the risk, when we reshuffles its values among the individuals, individual A gets B's value and B gets F's value and so on, then the predictive performance will deteriorate at least for many permutations. If the input is not a significant predictor of the risk, the accuracy will not decrease very much. For each input variable, I draw 5,000 random permutations. Let  $\alpha_i$  be the accuracy rate in the shuffled input data induced by the *i*-th permutation. Let m be the mean of these  $\alpha_i$ 's and sd the standard deviation. If  $\alpha > m + 2 * sd$ , I define the input strongly influential, denoted with \*\*\*. If it is not strongly influential but  $\alpha > m + sd$ , I define it to be moderately influential, denoted with \*\*. If it is not moderately influential but  $\alpha > m$ , I define it to be slightly influential, denoted with \*. Otherwise the input has no significant effect on the prediction accuracy. These influential levels are shown in [Table 4](#page-20-1). Note that these \*'s only mean that they have significant influence on predicting the outcome, but they do not tell us if the input is changed by a unit, how much will be the effect on the risk of the disease. This criterion for determining the influence of a variable may not work well if two input variables are highly correlated. This also applies to the p-value criterion used in the statistical model.

An important variable and the degree of its importance is marked with \*'s are almost identical to those in the statistical multinomial logit model above with the exception that two variables — childhood SES and College+ — show significant influence on the risks of diseases in other category and in comorbidity category.

<span id="page-20-2"></span><span id="page-20-1"></span>

Table 4: Influential variables for prediction of mid-age diseases

\*\*\* = strongly, \*\* = moderately, \* = slighly influential based on the criterion of m -3\*s.d., m - 2\*s.d. and m is greater than 0 respectively, where m is the mean and sd is the standard deviation calculated with 5000 random permutations for each variable.

## <span id="page-20-0"></span>**5.** Discussions

The above is a static model of health outcomes at one point of time in life-cycle, i.e. in early 50's. Health progression over time and the feedback effect of earlier health status and health behaviors on later health outcomes are also important to analyze from the healthcare and public policy perspectives. For analysis of pathways through health states, the statistical literature generally uses a multi-state time to event framework with Cox regression models capturing the effect of time varying covariates. In Raut  $(2017)$  and Raut  $(2021)$ , I have used such models for prediction of disease risks over time. A multi-state statistical model predicts the probability of disease incidence over many periods. These models assume a Markovian structure and assumes that covariates influence the probabilities of health outcomes through a linear aggregator  $X_t' \beta$  at time  $t$  in a Cox proportionality fashion, similar to the multinomial logit model in [Eq. \(1\).](#page-4-1) For estimation a method like maximum likelihood or partial likelihood and to derive sampling theory of the parameter estimates, these statistical models assume that the true data generating process is one of the member of the parametric or semi-parametric family. Like the question we addressed about the above static model, a similar question arises in this longitudinal case: Could a deep neural network model by relaxing the above restrictions on functional form and the data generating process perform <span id="page-21-0"></span>better than a statistical multi-state model?

A few papers([Faraggi and Simon, 1995](#page-25-10); [Biganzoli et al., 1998;](#page-24-9) [Katzman et al., 2018;](#page-25-11) [Lee et al., 2018](#page-26-10); [Ranganath et al., 2016\)](#page-26-11) used feed-forward MLP networks to compute the survival probabilities when there is only one possible transition between two health states alive and death–with the exception of [Lee et al. \(2018](#page-26-10)) who studied competing risks, by breaking death into various causes of death. [Katzman et al. \(2018](#page-25-11)) introduced a more general non-linearity of the covariate effects, but still kept the Cox proportionality assumption. [Ranganath et al. \(2016\)](#page-26-11) assumed parametric form for the baseline hazard function as compared to the non-parametric form in Cox model, but they made the covariate effects nonlinear. [Ren et al. \(2019\)](#page-26-12) consider a recurrent neural network, but the covariates are time-fixed at the initial time step. They also restricted to only one transition, i.e., a two-state model. None of these models deals with sequential framework where new information arise with time steps and update the previously estimated transition probability estimates. In these models, all the inputs from the past, present and the future times in the sample determine current probabilities. These models have no ways to store information learned from the past inputs. After training these models, when new data arrive, these models cannot use this new data to update the predicted probabilities without losing information in the early periods.

A recurrent neural network (RNN) uses feedback connections or self connection of neurons in the hidden layer, and thus is capable of storing important information learned in the past in these recurrent neurons. Like an MLP is a universal function approximator, an RNN has the similar nice property that with sufficiently large number of hidden recurrent neurons, an RNN can approximate any sequence-to-sequence mapping([Graves et al., 2014;](#page-25-12) [Hammer, 2000;](#page-25-13) [Siegelmann and Sontag, 1992\)](#page-26-13). These models have shared weights between time-steps and in the input and output layers, as a result when new data arrive after training the model, it can use all the past important information learned from the past to this new data point and predict the future probabilities in the light of this new data. Since training such models involve computation of gradients using backpropagation through time, it involves multiplication of numbers less than one many times, leading to vanishing gradient problem. In these scenarios, it cannot keep useful information in memory from the long time back. Overcoming these problems led to a few modifications of the RNN framework. The most successful of them is the long short memory (LSTM) RNN model introduced by [Hochreiter](#page-25-14) [and Schmidhuber \(1997](#page-25-14)). For more on LSTM-RNN models, see [Graves \(2012](#page-25-4)). I use this LSTM-RNN model for prediction of time-to-event probabilities of health outcomes.

<span id="page-22-1"></span>Another problem is with the training data size. To obtain good predictive performance, these models require a large number of training examples. In drug discovery problems or with surveys or lab experiments, obtaining large number of examples is costly. To overcome small data problem, [\(Altae-Tran, 2016](#page-24-10); [Altae-Tran et al., 2017\)](#page-24-11) introduced further refinement of the LSTM-RNN framework. I do not adopt such modifications.

In [Raut \(2020](#page-26-14)), I formulated an LSTM-RNN model of multi-state time-to-event model, implemented in Keras module of Tensorflow 2.0 for Python and compared its predictive performance with that of a multi-state statistical model. Similar to the accuracy rate as the criterion to evaluate performance of the models in multi-class classification given in perivious section, I used the *c-index* criterion to discriminate the performance of various models in predicting time-to-event probabilities. I found that a LSTM-RNN type neural network model did better job in predicting time-to-event probabilities than a multi-state statistical model.

## <span id="page-22-0"></span>**6.** Conclusion

This paper addresses two issues: First, to predict risks of diseases and to detect influential variables for these risks, how does a statistical multinomial logit model compare with a deep neural network model? Second, using the Health and Retirement Surveys data, the paper evaluates these two types of models and examines how early childhood factors, and health behaviors affect risks of diseases for adults in their early 50's. The paper considers four categories of chronic diseases: Cardiovascular, Cancer, single other disease, and comorbidity. The input variables used are dummy variables — White, Female, Childhood SES, Childhood Health, College+, High BMI, Smoking and Exercising — and continuous variables — CESD and Cognitive scores. The variable CESD is an aggregate measure of various stresses.

The paper explains that under strong assumptions on the true data generating process, the statistical models use maximum likelihood or similar optimizing methods to estimate parameters of the model, derive sampling properties of the estimates which provide criteria such as p-values and other hypothesis testing procedures to pick important variables and select a best model out a set of models. An estimated parameter in most models directly provides a numerical estimate of the quantitative effect of the associated variable on the risk

<span id="page-23-0"></span>of diseases. On the other hand, a deep neural network model has more general assumptions on the data generating process, but it does not have a good method to identify important variables and to estimate the numerical effect of a variable on the risks of various diseases. To identify the influential variables for prediction of risks in the deep neural network framework involving multinomial outcomes, this paper adapts the *permutation importance* technique of [Breiman \(2001b](#page-24-4)) which he introduced for random forests models.

The paper uses a common randomly drawn training dataset to fit both types of models and computes their predictive accuracy on a common disjoint test dataset and compares the predictive performance of the two models. The paper finds that the statistical multinomial logit model has an accuracy rate of 38.9 and the deep neural network model has a slightly higher accuracy rate of 39.4.

Both models pick the same variables as influential in the prediction of risks, with the exception that while the childhood SES and College+ variables are not statistically significant (i.e., not influential) in the statistical multinomial logit model, these two variables are influential in the deep neural network model for the prediction of risks of the single disease in the other category and for the risks of comorbidity. To get the quantitative effect of a variable on risks of diseases, the associated parameter estimate in statistical multinomial logit model directly provides that effect. Whereas, a deep neural network model does not have such straightforward estimate or interpretation of parameters.

From the fitted models, the paper finds that the childhood health, BMI and smoking habits have quite strong effects on risks of various diseases. More specifically, the paper finds that a high BMI individual has the risk of cardiovascular disease 1.95 times higher than the risk of cardiovascular disease of a low BMI individual. An individual who smokes has the risk of cancer 1.57 times higher than the risk of cancer of an individual who does not smoke.

While the performance of the deep neural network model in this paper does not show significant improvement in performance over the statistical multinomial logit model, [Raut](#page-26-14) [\(2020](#page-26-14)) formulated a deep LSTM type recurrent neural network (RNN) model of risk of diseases over time (i.e., time series of risks) and compared its performance with the statistical analogue, a multi-state time-to-event model. Both models were fitted using the Health and Retirement Survey data. [Raut \(2020](#page-26-14)) found that the deep LSTM-RNN model attained substantially higher performance compared to the statistical multi-state time-to-event model. It is possible that other type of deep neural network architectures such as convolutional neural network (CNN) architecture and a much bigger dataset with many more relevant variables may provide significantly better performance compared to the feed-forward deep neural network considered in this paper. Only more empirical research can tell.

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